

Iterated Algorithmic Bias in the Interactive Machine Learning Process of Information Filtering

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Keywords: Information Retrieval, Machine Learning, Bias, Iterative Learning.

Abstract: Early supervised machine learning (ML) algorithms have used reliable labels from experts to build predictions. But recently, these algorithms have been increasingly receiving data from the general population in the form of labels, annotations, etc. The result is that algorithms are subject to bias that is born from ingesting unchecked information, such as biased samples and biased labels. Furthermore, people and algorithms are increasingly engaged in interactive processes wherein neither the human nor the algorithms receive unbiased data. Algorithms can also make biased predictions, known as algorithmic bias. We investigate three forms of iterated algorithmic bias and how they affect the performance of machine learning algorithms. Using controlled experiments on synthetic data, we found that the three different iterated bias modes do affect the models learned by ML algorithms. We also found that Iterated filter bias, which is prominent in personalized user interfaces, can limit humans' ability to discover relevant data.

1 INTRODUCTION

Websites and online services offer large amounts of information, products, and choices. This information is only useful to the extent that people can find what they are interested in. There are two major adaptive paradigms aiming to help sift through information: information retrieval (Robertson, 1977; Spark, 1978) and recommender systems (Pazzani and Billsus, 1997; Cover and Hart, 1967; Koren et al., 2009; Abdollahi and Nasraoui, 2014; Goldberg et al., 1992; Nasraoui and Pavuluri, 2004; Abdollahi and Nasraoui, 2016; Abdollahi, 2017; Abdollahi and Nasraoui, 2017). All existing approaches aid people by suppressing information that is determined to be disliked or not relevant. Thus, all of these methods, by gating access to information, have potentially profound implications for what information people can and cannot find, and thus what they see, purchase, and learn.

Common to both recommender systems and information filters is: (1) selection of a subset of data about which people express their preference by a process that is not random sampling, and (2) an iterative learning process in which people's responses to the selected subset are used to train the algorithm for subsequent iterations. The data used to train and optimize performance of these systems are based on hu-

man actions. Thus, data that are observed and omitted are not randomly selected, but are the consequences of people's choices.

1.1 Iterated Learning and Language Evolution

In language learning, humans form their own mapping rules after listening to others, and then speak the language following the rules they learned, which will affect the next learner (Kirby et al., 2014). Language learning and machine learning have several properties in common. For example, a 'hypothesis' in language is analogous to a 'model' in machine learning. Learning a language which gets transmitted throughout consecutive generations of humans is analogous to learning an online model throughout consecutive iterations of machine learning.

Researchers have shown that iterated learning can produce meaningful structure patterns in language learning (Kirby et al., 2014; Smith, 2009). In particular, the process of language evolution can be viewed in terms of a Markov chain, as shown in Figure 1 (a). We should expect an iterated learning chain to converge to the prior distribution of all hypotheses given that the learner is a Bayesian learner (Griffiths and

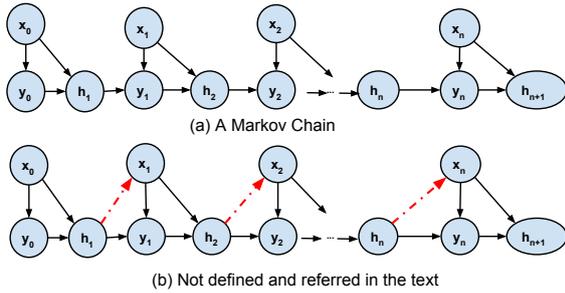


Figure 1: Illustration of iterated learning with (bottom) and without (top) dependency from previous iterations.

Kalish, 2005). That is, the knowledge learned is not accumulated during the whole process. We refer to this iterated learning model as *pure iterated learning (PIL)*.

1.2 Relationship between Iterated Algorithmic Bias and other Types of Bias

In statistics, bias refers to the systematic distortion of a statistic. Here we can distinguish a biased sample, which means a sample that is incorrectly assumed to be a random sample of a population, and estimator bias, which results from an estimator whose expectation differs from the true value of the parameter (Rothman et al., 2008). Within our scope, bias is closer to the sample bias and estimator bias from statistics; however, we are interested in what we call **iterated algorithmic bias** which is the dynamic bias that occurs during the selection by machine learning algorithms of data to show to the user to request labels in order to construct more training data, and subsequently update their prediction model, and how this bias affects the learned (or estimated) model in successive iterations.

Recent researches pointed to the need to pay attention to bias and fairness in machine learning (McNair, 2018; Goel et al., 2018; Friedler et al., 2018; Kleinberg et al., 2018; Dwork et al., 2018). Some research has studied different forms of biases, some are due to the algorithms while others are due to inherent biases in the input data or in the interaction between data and algorithms (Hajian et al., 2016; Baeza-Yates, 2016; Baeza-Yates, 2018; Lambrecht and Tucker, 2018; Garcia, 2016; Bozdag, 2013; Spinelli and Crovella, 2017; Chaney et al., 2017; Jannach et al., 2016). Some work studied biases emerging due to item popularity (Joachims et al., 2017; Collins et al., 2018; Liang et al., 2016; Schnabel et al., 2016). A recent work studied bias that is due to the assimilation bias in recommender systems (Zhang et al., 2017). Because

recommender systems have a direct impact on humans, some recent research studied the impact of polarization on biasing rating data (Badami et al., 2017) and proposed strategies to mitigate this polarization in collaborative filtering recommender systems (Badami et al., 2018) while other recent research pointed to bias emerging from continuous feedback loops between recommender systems and humans (Shafto and Nasraoui, 2016; Nasraoui and Shafto, 2016). Overall, the study of algorithmic bias falls under the umbrella of fair machine learning (Abdollahi and Nasraoui, 2018).

Taking all the above in consideration, we observe that most previous research has treated algorithmic bias as a static factor, which fails to capture the iterative nature of bias that is born from continuous interaction between humans and algorithms. We argue that algorithmic bias evolves with human interaction in an iterative manner, which may have a long-term effect on algorithm performance and humans' discovery and learning. We propose a framework for investigating the implications of interactions between humans and algorithms, that draws on diverse literature to provide algorithmic, mathematical, computational, and behavioral tools for investigating human-algorithm interaction. Our approach draws on foundational algorithms for selecting and filtering of data from computer science, while also adapting mathematical methods from the study of cultural evolution (Griffiths and Kalish, 2005; Beppu and Griffiths, 2009) to formalize the implications of iterative interactions.

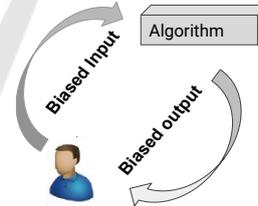


Figure 2: Evolution of bias between algorithm and human. A continuous interaction between humans and algorithms generates bias that we refer to as **iterated bias**, namely bias that **results from repeated interaction between humans and algorithms**.

In this study, we focus on simulating how the data that is selected to be presented to users affects the algorithm's performance (see Figure 2). In this work, we choose recommendation systems as the machine learning algorithm to be studied. One reason is that recommendation systems have more direct interaction options with humans, while information retrieval focuses on getting relevant information only. We further simplify the recommendation problem into a 2-class classification problem, namely, like/relevant (class 1)

or dislike/non-relevant (class 0), thus focusing on a personalized content-based filtering recommendation algorithm.

2 ITERATED ALGORITHMIC BIAS IN ONLINE LEARNING

Because we are interested in studying the interaction between machine learning algorithms and humans, we adopt an efficient way to observe the effect from both sides by using iterated interaction between algorithm and human action.

To begin, we consider three possible mechanisms for selecting information to present to users: **Random, Active-bias, and Filter-bias**. These three mechanisms simulate different regimes. Random selection is unbiased and will be used here purely as a baseline for no filtering. Active-bias selection introduces a bias whose goal is to accurately predict user's preferences. Filter-bias selection brings a bias whose goal is to provide relevant information or preferred items.

Before we go into the three forms of iterated algorithmic bias, we first investigate PIL. We adopt some of the concepts from Griffiths (Griffiths and Kalish, 2005). Consider a task in which the algorithm learns a mapping from a set of m inputs $X = \{x_1, \dots, x_m\}$ to m corresponding outputs $\{y_1, \dots, y_m\}$ through a latent hypothesis h . For instance, based on previous purchase or rating data (x, y) , a recommendation system will collect a new data about a purchased item (x_{new}, y_{new}) and update its model to recommend more interesting items to the users. Here, x represents the algorithm's selections and y represents people's responses (e.g. likes/dislikes). Following Griffiths' model for human learners, we assume a Bayesian model for prediction.

2.1 Iterated Learning with Iterated Filter-bias Dependency

The extent of the departure that we propose from a conventional machine learning framework toward a human - machine learning framework, can be measured by the contrast between the evolution of iterated learning *without* and *with* the added dependency (see Figure 1).

We used notation $q(x)$ to represent this independence. Here, $q(x)$ indicates an unbiased sample from the world, rather than a selection made by the algorithm. On the other hand, with the dependency, the algorithm at iteration n sees input x_n which is generated

from both the objective distribution $q(x)$ and another distribution $p_{seen}(x|h_n)$ that captures the dependency on the previous hypothesis h_n which implies future bias of what can be seen by the user. Thus, the probability of input item x is given by:

$$p(\mathbf{x}|h_n) = (1 - \epsilon)p_{seen}(\mathbf{x}|h_n) + \epsilon q(\mathbf{x}) \quad (1)$$

Here ϵ is the weight of two factors which control the data that algorithm will see. Recall that the probability of seeing an item is related to its rank in a rating based recommendation system or an optimal probabilistic information filter (Robertson, 1977). In most circumstances, the recommendation system has a preferred goal, such as recommending relevant items (with $y=1$). Then x will be chosen based on the probability of relevance $p(y = 1|x, h_n)$, $x \in X$. Assume that we have a candidate pool X at time n (In practice X would be the data points or items that the system can recommend at time n), then

$$p_{seen}(\mathbf{x}|h_n) = \frac{p(\mathbf{y} = 1|\mathbf{x}, h_n)}{\sum_{\mathbf{x} \in X} p(\mathbf{y} = 1|\mathbf{x}, h_n)} \quad (2)$$

The selection of inputs depends on the hypothesis, and therefore information is not unbiased, $p(\mathbf{x}|h_n) \neq q(\mathbf{x})$. The derivations of the transition probabilities in Eq. 2 will be modified to take into account Eq. 1, and will become

$$p(h_{n+1}|h_n) = \sum_{\mathbf{x} \in X} \sum_{\mathbf{y} \in Y} p(h_{n+1}|\mathbf{x}, \mathbf{y}) p(\mathbf{y}|\mathbf{x}, h_n) p_{seen}(\mathbf{x}|h_n) \quad (3)$$

Eq. 3 can be used to derive the asymptotic behavior of the Markov chain with transition matrix $T(h_{n+1}) = p(h_{n+1}|h_n)$, i.e.

$$p(h_{n+1}) = \epsilon p(h_{n+1}) + (1 - \epsilon) T_{bias} \quad (4)$$

Here, T_{bias} is:

$$\left[\sum_{\mathbf{x} \in X} \sum_{\mathbf{y} \in Y} p(h_{n+1}|\mathbf{x}, \mathbf{y}) \sum_{h_n \in H} p(\mathbf{y}|\mathbf{x}, h_n) p_{seen}(\mathbf{x}|h_n) \right] p(h_n) \quad (5)$$

Thus, iterated learning with filter bias converges to a mixture of the prior and the bias induced by filtering. To illustrate the effects of filter bias, we can analyze a simple and most extreme case where the filtering algorithm shows only the most relevant data in the next iteration (e.g. top-1 recommender). Hence

$$x^{top} = \underset{x}{\operatorname{argmax}} P(y|x, h) \quad (6)$$

$$p_{seen}(\mathbf{x}|h_n) = \begin{cases} 1 & \text{for } x = x^{top} \\ 0 & \text{otherwise} \end{cases} \quad (7)$$

$$T_{bias} = \left[\sum_{\mathbf{x} \in X} \sum_{\mathbf{y} \in Y} p(h_{n+1}|\mathbf{x}, \mathbf{y}) \sum_{h_n \in H} p(\mathbf{y}|\mathbf{x}_n^{top}, h_n) \right] p(h_n) \quad (8)$$

Based on equation 3, the transition matrix is related to the probability of item x being seen by the user, which is the probability of belonging to class $y = 1$. The fact that x_n^{top} maximizes $p(y|x, h)$ suggests limitations to the ability to learn from such data. Specifically, the selection of relevant data allows the possibility of learning that an input that is predicted to be relevant is not, but does not allow the possibility of learning that an input that is predicted to be irrelevant is actually relevant. In this sense, **selection of evidence based on relevance is related to the confirmation bias in cognitive science**, where learners have been observed to (arguably maladaptively) select data which they believe to be true (i.e. they fail to attempt to falsify their hypotheses) (Klayman and Ha, 1987). **Put differently, recommendation algorithms may induce a blind spot where data that are potentially important for understanding relevance are never seen.**

2.2 Iterated Learning with Iterated Active-bias Dependency

Active learning was first introduced to reduce the number of labeled samples needed for learning an accurate predictive model, and thus accelerate the speed of learning towards an expected goal (Cohn et al., 1996). Instead of choosing random samples to be manually labeled for the training set, the algorithm can interactively query the user to obtain the desired data sample to be labeled (Settles, 2010).

$$p_{active}(\mathbf{x}|h) \propto 1 - p(\hat{y}|\mathbf{x}, h) \quad (9)$$

where $\hat{y} = \arg \max_y (p(y|\mathbf{x}, h))$. Given \mathbf{x} and h , \hat{y} aims to select the most certain predicted label, whether it is class $y=0$ or class $y=1$. Hence in Eq. 9, \mathbf{x} values are selected to be the least certain about \hat{y} , the predicted y value.

Assuming a simplified algorithm where only the very uncertain data are selected, we can investigate the limiting behavior of an algorithm with the active learning bias. Assuming a mixture of random sampling and active learning, we obtain:

$$x^{act} = \arg \max_x (1 - p(\hat{y}|\mathbf{x}, h)) \quad (10)$$

$$p(h_{n+1}) = \epsilon p(h_{n+1}) + (1 - \epsilon) T_{active} \quad (11)$$

Where

$$T_{active} = \left[\sum_{\mathbf{x} \in X} \sum_{y \in Y} p(h_{n+1}|\mathbf{x}, y) \sum_{h_n \in H} p(y|\mathbf{x}_n^{act}, h_n) \right] p(h_n) \quad (12)$$

The limiting behavior depends on the iterated active learning bias, \mathbf{x}_n^{act} . This is, in most cases, in

opposition to the goal of filtering, the algorithm will only select data point(s) which are closest to the learned model's boundary, if we are learning a classifier for example. In contrast, the filtering algorithm is almost certain to pick items that it knows are relevant.

2.3 Iterated Learning with Random Selection

The iterated random selection is considered as a trivial baseline for comparison purposes. This selection mechanism randomly chooses instances to pass to the next learner during iterations.

2.4 Evaluating the Effect of Iterated Algorithmic Bias on Learning Algorithms

In order to study the impact of iterated bias on an algorithm, we compute three properties: the blind spot, boundary shift, and the Gini coefficient. These properties are defined below.

2.4.1 Blind Spot

The *blind spot* is defined as the set of data available to a relevance filter algorithm for which, the probability of being seen by the human interacting with the algorithm that learned the hypothesis h , is less than δ :

$$\mathbf{D}_\delta^F = \{\mathbf{x} \in X \mid p_{seen}(\mathbf{x}|h) < \delta\} \quad (13)$$

In the real world, some data can be invisible to some users because of bias either from users or from the algorithm itself. Studying blind spots can enhance our understanding about the impact of algorithmic bias on humans. In addition, we define the *class-1-blind spot* or *relevant-item-blind spot* as the data in the blind spot, with true label $y = 1$

$$\mathbf{D}_\delta^{F+} = \{\mathbf{x} \in \mathbf{D}_\delta^F \text{ and } y = 1\} \quad (14)$$

Note that the blind spot in Eq. 13 is also called *all-classes-blind spot*.

2.4.2 Boundary Shift

Boundary shift indicates how different forms of iterated algorithmic bias affect the model h that is learned by an algorithm. It is defined as the number of points that are predicted to be in class $y = 1$ given a learned model h :

$$b = \sum_{x \in X} p(y = 1|x, h) \quad (15)$$

Here b is the number of points that are predicted as class $y = 1$ given a learned model h . This number helps to quantify the extent of shift in the boundary as a result of different bias modes.

2.4.3 Gini Coefficient

We also conduct a Gini coefficient analysis on how boundary shifts affect the inequality of predicted relevance for the test set. Let $p_i = p(y = 1|x_i, h)$. For a population with n values p_i , $i = 1$ to n , that are indexed in non-decreasing order ($p_{(i)} \leq p_{(i+1)}$). The Gini coefficient can be calculated as follows (Stuart et al., 1994):

$$G = \left(\frac{\sum_{i=1}^n (2i - n - 1)p_{(i)}}{n \sum_{i=1}^n p_{(i)}} \right) \quad (16)$$

The higher the Gini coefficient, the more unequal are the frequencies of the different labels. The Gini coefficient is used to gauge the impact of different iterated algorithmic bias modes on the heterogeneity of the predicted probability in the relevant class during human-machine learning algorithm interaction.

3 EXPERIMENTS

As stated in section 3, we mainly focus on a two-class model of recommendation in order to perform our study. In this situation, any classical supervised classification could be used in our model (Domingos and Pazzani, 1997; Hosmer Jr et al., 2013; Cortes and Vapnik, 1995). For the purpose of easier interpretation and visualization of the boundary and to more easily integrate with the probabilistic framework in section 2, we chose the Naive Bayes classifier.

Synthetic Data: A 2D data set (see figure 3) was generated from two Gaussian distributions corresponding to classes $y \in \{0, 1\}$ for like (relevant) and dislike (non-relevant), respectively. Each class contains 1000 data points centered at $\{-2, 0\}$ and $\{2, 0\}$, with standard deviation $\sigma = 1$. The data set is then split into the following parts: **Testing set:** used as a global testing set (200 points from each class); **Validation set:** used for the blind spot analysis (200 points from each class). Note that the subset is similar to the testing set, however we only use this one for blind spot analysis to avoid confusion; **Initializing set:** used to initialize the first boundary (we tested initialization with class 1/class 0 ratios as follows: 100/100). Note that initialization set can also be called initial training set; **Candidate set:** used as query set of data which will be gradually added to the training set (points besides the above three groups that will be added to the candidate set).

The reason why we need the four subsets is that we are simulating a real scenario with interaction between humans and algorithms. Part of this interaction will include picking query data items and labeling them, thus augmenting the training set. Thus,

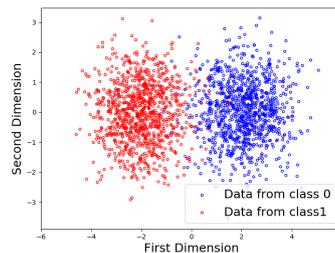


Figure 3: Original data with two classes.

to avoid depleting the testing set, we need to isolate these query items in the separate “candidate pool”. A similar reason motivates the remaining separate subsets in order to keep their size constant throughout all the interactions of module learning.

Methods: We wish to simulate the human-algorithm interaction at the heart of recommendation and information filtering. To do so, we initialize the models following the initialization set. Then, we explore three forms of iterated algorithmic bias modes (see Section 2). We simulate runs of 200 iterations where a single iteration is comprised of the algorithm providing a recommendation, the user labeling the recommendation, and the algorithm updating its model of the user’s preferences. Each combination of parameters yields a data set that simulates the outcome of human and algorithm interacting. We simulate this whole process 40 times independently, which generates the data that we will use to investigate several research questions.

4 RESULTS

The key issue is to study whether and how information filtering may lead to systematic biases in the learned model, as captured by the classification boundary. Based on the three metrics introduced in section 2.4, we ask the question: **How does iterated algorithmic bias affect the learned categories?**

To answer this question, we adopt four different investigating approaches. First, we will compare the inferred boundaries after interaction to the ground truth boundaries. Second, we will focus on the effects of iteration alone by analyzing the boundary before interaction and after. Third, We use the Gini coefficient to measure the heterogeneity or inequality of the predicted label distribution in the testing set. Fourth, we investigate the size of the blind spot induced by each of the iterated algorithmic bias modes. Together, these will describe the outcomes of algorithmic bias, in terms of the induced blind spot.

RQ 1: Do Different Forms of Iterated Algo-

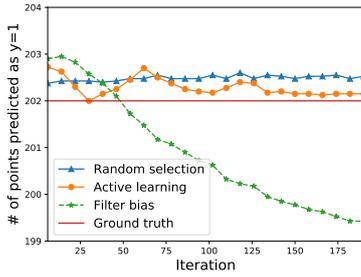


Figure 4: Boundary shift (Eq. 15) based on the three iterated algorithmic bias forms. The y axis is the number of testing points which are predicted to be in class $y=1$. The iterated filter bias diverges from the ground truth significantly with more iterations.

Algorithmic Bias Have Different Effects on the Boundary Shift? To answer this question, We assume that the initialization is balanced between both classes. As shown in Eq. 1, we here assume that $q(x)$ is identical for all data points, thus we can ignore the second part of the equation, i.e. the probability of being seen is only dependent on the predicted probability of candidate points. Note that we could get some prior probability of X_i , in which case we could add this parameter to our framework. Here, we assume them to be the same, hence we set $\epsilon = 0$.

We wish to quantify differences in the boundary between the categories as a function of the different algorithmic biases. To do so, we generate predictions for each test point in the test set by labeling each point based on the category that assigns it highest probability. We investigate the proportion of test points with the relevant label $y = 1$ at two time points: prior to human-algorithm interactions (immediately after initialization), and after human algorithm interactions. Note that we use ‘FB’ to represent filter bias, ‘AL’ for active learning bias, and ‘RM’ for random selection.

We run experiments with each of the three forms of algorithm bias, and compare their effect on boundary shifts. We also report the effect size based on *Cohen d* (Cohen, 1988). In this experiment, the effect size (ES) is calculated by $ES = (Boundary_{t=0} - Boundary_{t=200}) / std(\cdot)$, here $std(\cdot)$ is the standard deviation of the combined samples. We will use the same strategy to calculate the effect size in the rest of this paper. The results indicate significant differences for the filter bias condition ($p < .001$ by Mann-Whitney test or t-test, effect size = 1.96). In contrast, neither the Active Learning, nor the Random conditions resulted in statistically significant differences ($p = .15$ and $.77$ by Mann-Whitney test, or $p = .84$ and 1.0 by t-test; effective sizes $.03$ and 0.0 , respectively).

To illustrate this effect, we plot the number of points assigned to the target category versus ground-

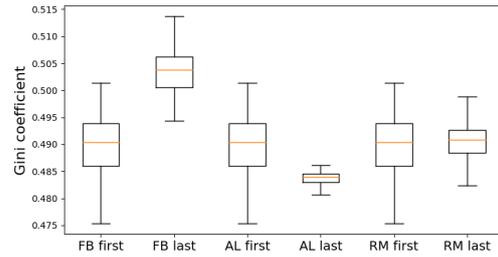


Figure 5: Box-plot of the Gini coefficient resulting from three forms of iterated algorithmic bias. The x-axis is the iterated algorithmic bias modes. ‘First’ means the first iteration ($t=0$), while ‘last’ indicates the last iteration ($t=200$). An ANOVA test across these three iterated algorithmic bias forms shows that the Gini index values are significantly different. The p-value from the ANOVA test is close to 0.000 (<0.05), which indicates that the three iterated algorithmic bias forms have different effects on the Gini coefficient.

truth for each iteration. Figure 4 shows that random selection and active learning bias converge to the ground-truth boundary. Filter bias, on the other hand, results in decreasing numbers of points predicted in the target category class 1, consistent with an overly restrictive category boundary.

RQ 2: Do Different Iterated Algorithmic Bias Modes Lead to Different Trends in the Inequality of Predicted Relevance throughout the Iterative Learning Given the Same Initialization? To answer this question, we run experiments with different forms of iterated algorithmic bias, and record the Gini coefficient when a new model is learned and applied to the testing set during the iterations.

Although the absolute difference between the first iteration and the last iteration is small (see Figure 5), a one-way ANOVA test across these three iterated algorithmic bias forms shows that the Gini index values are significantly different. The p-value from the ANOVA test is close to 0.000 (< 0.05), which indicates that the three iterated algorithmic bias forms have different effects on the Gini coefficient.

Interpretation of this Result: Given that the Gini coefficient measures the inequality or heterogeneity of the distribution of the relevance probabilities, this simulated experiment shows the different impact of different iterated algorithmic bias forms on the heterogeneity of the predicted probability to be in the relevant class within human machine learning algorithm interaction. Despite the small effect, the iterated algorithmic bias forms affect this distribution in different ways, and iterated filter bias causes the largest heterogeneity level as can be seen in Figure 5. The fact that filtering increases the inequality of predicted relevance means that filtering algorithms may increase the gap between liked and unliked items, with a pos-

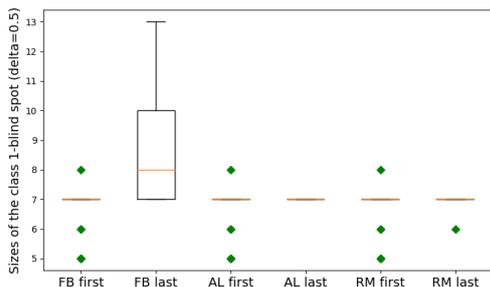


Figure 6: Box-plot of the size of the class-1-blind spot for all three iterated algorithmic bias forms. In this figure, the x-axis is the index of the three forms of iterated algorithms biases, ‘First’ means the first iteration ($t=0$), while ‘last’ indicates the last iteration ($t=200$). As shown in this box-plot, the initial class-1-blind spot is centered at 7. This is because the 200 randomly selected initial points from both classes force the boundary to be similar regardless of the randomization.

sible impact on polarizing user preferences.

RQ 3: Does Iterated Algorithmic Bias Affect the Size of the Class-1-blind Spot, i.e. is the Initial Size of the Blind Spot D_8^F Significantly Different Compared to Its Size in the Final Iteration? The blind spot represents the set of items that are much less likely to be shown to the user. Therefore this research question studies the significant impact of an extreme filtering on the number of items that can be seen or discovered by the user, within human - algorithm interaction. If the size of the blind spot is higher, then iterated algorithmic bias results in hiding items from the user. In the case of the blind spot from class 1, this means that even relevant items are affected.

We run experiments with $\delta = 0.5$, and record the size of the class-1-blind spots with three different iterated algorithmic bias forms. Here, we aim to check the effect of each iterated algorithmic bias form. As shown in Table 1, filter bias has significant effects on the class-1-blind spot, while random selection and active learning do not have a significant effect on the class-1-blind spot size (see Figure 6). The negative effect from iterated filter bias implies a large increase in the class 1 blind spot size, effectively hiding a significant number of ‘relevant’ items.

Interpretation of this Result: Given that the blind spot represents the items that are much less likely to be shown to the user, this simulated experiment studies the significant impact of an extreme filtering on the number of items that can be seen or discovered by the user, within human-machine learning interaction. Iterated filter bias effectively hides a significant number of ‘relevant’ items that the user misses out on compared to AL. AL has no significant impact on the relevant blind spot, but increase the all-class

Table 1: Results of the Mann-Whitney U test and t-test comparing the size of the class-1-blind spot for the three forms of iterated algorithmic bias. Bold means significance computed at $p < 0.05$. The effect size is as $(BlindSpot|_{t=0} - BlindSpot|_{t=200}) / std(\cdot)$. The negative effect size shows that filter bias increases the class-1-blind spot size. For active learning bias, the p-value indicates the significance, however the effect size is small. Random selection has no significant effect.

	Filter Bias	Active Learning	Random Selection
Mann test p-value	$2.4e - 10$	0.03	0.06
t-test p-value	$2.2e - 10$	0.03	0.06
effect size	-1.22	-0.47	-0.4

blind spot to certain degree. Random selection has no such effect.

4.1 Results for Higher Dimensionality Data Sets

We performed similar experiments on 3D and 4D synthetic data using a similar data generation method. Our experiments produced similar results to the 2D data. We found that as long as the features are independent from each other, similar results are obtained to the 2D case above. One of the possible reason is that when features are independent, we can reduce them in a similar way to the 2D synthetic data set, i.e., one set of features highly related to the labels and another set of features non-related to the labels. Another possible reason is that independent features naturally fit the assumption of the Naive Bayes classifier. Finally, we generated a synthetic data with 10 dimensions, centered at $(-2, 0, 0, 0, 0, 0, 0, 0, 0, 0)$ and $(2, 0, 0, 0, 0, 0, 0, 0, 0, 0)$ with zero covariance between any two dimensions. We follow the same procedure as the 2D synthetic data. Table 2 shows that the 10D synthetic data leads to similar results to the 2D synthetic data set. To conclude, repeated experiments on additional data with dimensionality ranging from 2D to 10D led to the same conclusions that we have discussed for the 2D data set.

5 CONCLUSIONS

We investigated three forms of iterated algorithmic bias (filter, active learning, and random) and how they affect the performance of machine learning algorithms by formulating research questions about the impact of each type of bias. Based on statistical analysis of the results of several controlled experiments

Table 2: Experimental results with 10D synthetic data set. The effect size is calculated by $(Measurement|_{t=0} - Measurement|_{t=200})/std(\cdot)$. The measurements are the three metrics in section 2.4. We report the paired t-test results. For filter bias mode (FB), the results are identical to those of the 2D synthetic data across all three research questions. Active learning bias (AL) generates the same result as for the 2D synthetic data. Random selection (RM) has no obvious effect, similarly to the 2D synthetic data experiments.

	Bias type	Boundary Shift (p-value, ES)	Blind spot (p-value, ES)	Inequality (p-value, ES)
Statistical test	FB	(8e-15, 1.4)	(3e-13, -1.4)	(1.8e-13, -1.6)
	AL	(0.68, -0.09)	(0.5, 0.15)	(1.8e-15, 1.63)
	RM	(0.17, 0.17)	(0.1, -0.3)	(0.8, -0.01)

using synthetic data, we found that:

1) The three different forms of iterated algorithmic bias (filter, active learning, and random selection, used as query mechanisms to show data and request new feedback/labels from the user), **do affect algorithm performance** when fixing the human interaction probability to 1.

2) Iterated filter bias has a more significant effect on the class-1-blind spot size compared to the other two forms of algorithmic biases. **This means that iterated filter bias, which is prominent in personalized user interfaces, can limit humans' ability to discover data that is relevant to them.**

3) Iterated filter bias increases the inequality of predicted relevance. **This means that filtering algorithms may increase the gap between liked and unliked items, with a possible impact on polarizing user preferences.**

In this paper, we showed preliminary results on synthetic data. In real life, however, we have more complicated data. Thus, we are motivated to conduct experiments on real data in our future work. We also plan to study more research questions related to various modes of algorithmic bias.

ACKNOWLEDGEMENTS

This work was supported by National Science Foundation grant NSF-1549981.

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